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Reg. No. :	14. State and prove the additive property of Poisson
2012-5	
Name :	

IV Semester B.A./B.Sc./B.Com./B.B.A./B.B.A.T.T.M./B.B.M./B.C.A./B.S.W./ B.A. Afsal UI Ulama Degree (CCSS – Reg./Supple./Improv.) Examination, April 2012 CORE COURSE IN STATISTICS 4B 04STA : Probability Distribution

Time : 3 Hours

Max. Weightage: 30

(Weightage 1)

Instruction : Use of calculators and statistical tables are permitted.

PART-A

Answer any ten questions :

- 1. If a R.V. X follows uniform distribution over (-1, 1) What is its mean?
- 2. If a R.V. X follows B.D. (6, p) and if P(X = 2) = 9 P(X = 4) find p.
- 3. What is mean of a geometric distribution with parameter P.
- 4. If the m.g.f. of a R.V. X is given by  $M_x^{(t)} = e^{10t+2\sigma^2}$  find variance of X.
- 5. State Cauchy-Schwart's inequality.
- 6. If X is a R.V. such that E(X) = 3 and  $E(X^2) = 13$ . Find P {|X 3| < 5}
- 7. State central limit theorem.
- 8. If X follows N(0, 1), what is the distribution of  $X^2_{\cdot, \sqrt{\gamma}} \stackrel{\gamma}{\to} 0$
- 9. Define convergence in probability.
- 10. What is the coefficient of variation of Poisson distribution with parameters  $\lambda$  ?
- 11. What is simulation?

### PART-B

Answer any six questions from Part B.

- 12. If X has discrete uniform distribution over 1, 2, ....n, find its mean and variance.
- 13. Find the distribution of the sum of identically and independently distributed R.Vs. following geometric distribution.

## M 786

 $(10 \times 1 = 10)$ 

# (Weightage 2 each)

#### M 786

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- 14. State and prove the additive property of Poisson distribution.
- 15. If X follows normal distribution with mean = 12 and variance = 2, find P(9.8 < X < 13.8).
- 16. State the properties of normal distribution.
- 17. For a Binomial distribution mean = 4 and variance = 3, find its mode.
- 18. If the p.d.f. of a R.V. X is  $f(x) = e^{-x}$ ; x > 0 find P (|x 2| > 2) by Tchebyshev's inequality.
- 19. State and prove Bernoulli's law of large numbers.
- 20. How will you generate a geometric random variable in simulation ? (6×2=12)

## PART-C

Answer any 2 questions.

- 21. State and prove Tchebyshev's inequality.
- 22. Stating the conditions clearly, prove that Poisson distribution is the limiting form of Binomial distribution.
- 23. For a normal distribution 31% of the items are below 45 and 8% are above 64. Find the mean and standard deviation of the distribution.
- 24. a) Derive the m.g.f. of Gamma distribution. Hence find its mean and variance.
  - b) Find the distribution of the sum of two independent Gamma variates with parameters  $p_1$  and  $p_2$ .

(Weightage 4 each)

 $(2 \times 4 = 8)$